# OpticNet: Self-Adjusting Networks for ToR-Matching-ToR Optical Switching Architectures

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Abstract—Demand-aware reconfigurable datacenter networks can be modeled as a ToR-Matching-ToR (TMT) two-layer architecture, in which each top-of-rack (ToR) is represented by a static switch, and n ToRs are connected by a set of reconfigurable optical circuit switches (OCS). Each OCS internally connects a set of in-out ports via a matching that may be updated at runtime. The matching model is a formalization of such networks, where the datacenter topology is defined by the union of matchings over the set of nodes, each of which can be reconfigured at unit cost.

In this work we propose a scalable matching model for scenarios where OCS have a constant number of ports. Furthermore, we present OpticNet, a framework that maps a set of n static ToR switches to a set of p-port OCS to form any constant-degree topology. We prove that OpticNet uses a minimal number of reconfigurable switches to realize any desired network topology and allows to apply any existing self-adjusting network (SAN) algorithm on top of it, also preserving amortized performance guarantees. Our experimental results based on real workloads show that OpticNet is a flexible and efficient framework to design efficient SANs.

Index Terms—Reconfigurable Datacenter Networks, Self-Adjusting Networks, Optical Circuit Switching, Matching Model

## I. INTRODUCTION

The design of efficient datacenter networks has received increasing attention in recent years [1]–[9], fueled by datacentric online applications, such as web search, social networks, and multimedia. Augmenting the internal switching capacity of the datacenter networks according to traffic growth has become increasingly cost prohibitive [8]. Traditionally, datacenter network designs rely on static topologies, such as the Clos topology [10], [11], hypercubic topologies like BCube and MDCube [12], [13], or expander-based networks [14], [15]. Alternatively, rotor switches [8], [9] provide periodic direct connectivity. While such architectures perform well for all-to-all traffic patterns, they essentially form demand-oblivious topologies.<sup>1</sup>

Empirical studies show that communication patterns in datacenters feature much spatial and temporal locality [2], [3], [16], i.e., traffic is bursty and traffic matrices skewed. This structure represents an untapped potential for building more efficient communication networks This is the advantage of demand-aware topologies, based on e.g. 3D MEMS optical circuit switches (OCS) [1]–[5], [5]–[7], [17]–[19], which can

<sup>1</sup>Our research work was supported by CAPES, CNPq, Fapemig, and the European Research Council (ERC), grant agreement No. 864228.

provide shortcuts to such elephant flows. OCS provide reconfigurations in order of milliseconds and are reconfigurable ondemand, such that a scheduling or matching algorithms can determine the next configuration based on the network state. Several prototypes based on commodity-off-the-shelf OCS have been built, and their advantages have been demonstrated, e.g., [5], [19].

Self-Adjusting Networks (SAN) are networks which optimize their physical topology toward the demand they serve in an online manner, i.e., without prior knowledge of the traffic demand. SAN can be approached from the perspective of selfadjusting data structures [2]. This paradigm shift resembles the process that data structures went through some decades ago [20], [21], evolving from static worst-case designs toward demand-aware and self-adjusting data structures.

When analyzing the performance of SANs, it is common to distinguish between the so-called adjustment cost and service cost. The former refers to the cost of network reconfiguration (e.g., energy, latency and control plane overhead due to physical network topology adjustments), and the latter refers to the price of serving each communication request (e.g. the delay proportional to source-destination route length). Most of the existing SAN algorithms [2] have been based on edgedistance adjustment cost models, which define adjustment cost as the number of edges replaced between consecutive network topologies. This is a useful basic model that enabled the first algorithmic results. In practice, however, switching hardware usually allows to reconfigure the topology on a so-called permatching granularity, i.e., the adjustment cost is proportional to the number of OCS reconfigurations, where each switch internally connects its in-out ports via a matching.

ToR-Matching-ToR (TMT) [22] is a two-layer leaf-spine architecture for datacenter networks, in which each top-of-rack (ToR) is represented by a (leaf) static packet switch, and n ToRs are connected by a set of (spine) reconfigurable OCSs. Each spine switch internally connects n in-out ports via a *matching* that may be reconfigured at runtime. TMT can be used to model existing systems, such as RotorNet [9], Opera [8], and ProjecToR [3].

The matching model (MM) is a first formalization of TMT networks [22]. The key property of MM is assuming that any topology can be defined as a union of matchings over the set of nodes and that rearranging the edges of a single matching comes at a fixed cost. Thus the total *adjustment cost* for

adjusting the whole topology to a new one is determined by the number of matchings needed to construct the topology. Early work has shown this model's relevance, e.g. in [23] the authors simulate several so-called lazy SANs in the MM, based on spaced out (less frequent) calls of existing (sequential) SANs, such as SplayNets [4] and ReNets [24].

In this work, we propose a scalable matching model (MM'), which generalizes the MM by adding the constraint that the number of input-output ports of each reconfigurable spine switch is constant, while relaxing the constraint that the number of spine switches is constant. MM' adds flexibility to the network design, depending on the cost and constraints on available switching hardware. MM' uses larger leave-layer (static) switches, which typically come at a lower per-port hardware price than reconfigurable OCS hardware [25], and a greater number of smaller spine-layer switches, which can be incrementally appended to the existing architecture (even at runtime) in case new ToRs are added to the datacenter.

Summary of contributions: In Section II we describe the scalable matching model (MM'), a generalization of the matching model [22], that allows to model TMT architectures in which the number of ToRs (arbitrarily) exceeds the number of in-out ports of the spine-layer switches. In Section III we present OpticNet, a framework that maps a set of (leavelayer) ToR switches to a set of (spine-layer) demand-aware reconfigurable OCSs to form any constant-degree network topology. In Section V we prove that OpticNet is correct, is optimal with respect to the number of spine switches, and any existing SAN algorithm can run on top of it, while preserving amortized performance guarantees in the MM' model. In Section VI we describe the implementation of OpticNet and evaluate its performance in combination with state-of-the-art SAN algorithms. Finally, in Section VII we discuss related work, and in Section VIII present our conclusions.

#### II. MODEL

**SANs:** The objective of SAN algorithms is to create a network topology to connect a set V of n communication nodes (e.g., top-of-rack switches, ToRs). The input to the problem is given by a sequence  $\sigma$  of m messages  $\sigma_i(s_i, d_i) \in V \times V$  occurring over time, with source  $s_i$  and destination  $d_i$ ; m can be infinite. We denote by  $b_i$  the time when a message  $\sigma_i$  is generated, and by  $e_i$  the time in which it is delivered. The sequence  $\sigma$  is revealed over time, in an online manner, and can be arbitrary (e.g. chosen adversarially). When serving these communication requests, the network can adjust over time, through a sequence of network topologies  $N_0, N_1, \ldots$ . Each  $N_t$  should belong to some desired graph family N. For scalability reasons, the networks should be of *constant degree*.

Adjustments: In order to minimize the communication cost and adjust the topology smoothly over time, the network is reconfigured (locally) through adjustments that preserve the desired properties of the graph family  $\mathcal{N}$ . SANs like SplayNet [4] and DiSplayNet [26] are based on Binary Search Trees (BST) and extend the classical *zig*, *zig-zig* and *zig-zag* rotations, first introduced for splay trees [20]. CBTrees [27] and CBNet [28] leverage *bottom-up* and *top-down* semi-splaying (*semi-zigzig* and *semi-zigzag*). Each splay operation updates a constant number of links at constant cost, and roughly halves the depth of every node along the communication path. This halving effect makes splaying efficient in an amortized sense.

**TMT:** TMT [22] is a useful architecture to model RDN. It is a two-layer network, in which a set of *static* leaf-layer (ToR) switches is connected using a set of *reconfigurable* spine-layer switches (OCS). Each OCS internally connects its in-out ports via a *matching*, that can be dynamic and change over time.

**MM:** The matching model [22] is a formalization of the TMT architecture. The network consists of a set of *n* nodes (leaf layer static switches) are connected using k' = O(1) (spine-layer reconfigurable) switches, SW = $\{sw_1, sw_2, \ldots, sw_{k'}\}$ , and each switch internally connects its *n in-out ports* via a *matching*. At each time *t*, the network is the union of these matchings:  $N_t = \mathcal{M}_t = \bigcup_{i=1}^k M(i, t)$ , where M(i, t) denotes the matching on switch  $sw_i$  at time *t*.

Scalable matching model (MM'): In this work, we generalize the MM by adding the constraint that the number of ports of each spine-layer switch is constant, while relaxing the constraint that the number of spine switches is constant. Let  $\mathcal{N}$  be the family of constant degree ( $\leq k$ ) graphs on a set Vof n nodes (static leaf-layer ToR switches) and  $\mathcal{N}_t \in \mathcal{N}$  be a network topology at time t. Let  $SW = \{sw_1, \ldots, sw_{n'}\}$ be a set of (reconfigurable spine-layer) switches, of size n' = f(n, p, k), where each switch  $sw_i \in SW$  internally connects its p = O(1) in-out ports via a matching M(i, t) of size  $\leq p$ . As in MM, at each time t, the network  $N_t$  is equal to the union of all these matchings:

$$N_t = \mathcal{M}_t = \bigcup_{i=1}^{n'} M(i, t).$$

**TMT port configuration:** The port-to-port physical connections between leaf and spine layers in a TMT architecture can be realized in different ways, according to the hardware specification (e.g., via free-space optics [3]). In this work, we assume that leaf-spine connections are static *half-duplex* links<sup>2</sup>, i.e., for two ToRs (leaf-layer switches)  $(u, v) \in N_t$  to establish a connection, we need that  $\exists sw_x \in SW | (u, v) \in M(x, t)$ . Moreover, there must be a static (physical) link connecting an output port of u to an input port of  $sw_x$  and a static link from an output port of  $sw_x$  to an input port of v.

Before the system (RDN) starts operating, the TMT architecture must be configured according to these requirements, i.e., we need to find a one-to-one assignment, each representing a half-duplex link, between all in-out and out-in ports of leaf-spine switch pairs.

In the MM, the port mapping between leaf-layer and spinelayer switches is straightforward: each ToR  $i, 1 \le i \le n$  has k' uplinks, where uplink  $j, 1 \le j \le k'$  connects to port i in  $sw_j$ . The directed outgoing (leaf) uplink is connected to the incoming port of the (spine) switch and the directed incoming

 $<sup>^{2}</sup>$ Note that a half-duplex configuration can be converted to full-duplex by using the same ToR-to-Switch configuration but letting go of the notions of input and output ports. This uses the ceiling of half of number of switches used by the half-duplex configuration

(leaf) uplink is connected to the outgoing port of the (spine) switch. Each switch has n input ports and n output ports and the connections are directed, from input to output ports. At any point in time, each switch  $sw_j \in SW$  provides a matching of size  $\leq n$  between its input and output ports.

In MM', however, because spine-layer switches are limited to a constant number of in-out ports, the problem of connecting leaf-layer and spine-layer switches has a different structure.

**MM' port mapping problem (MM'-PMP):** Let  $\mathcal{N}$  be the family of constant degree  $(\leq k)$  graphs on a set V of n nodes (static leaf-layer ToR switches), and  $SW = \{sw_1, \ldots, sw_{n'}\}$  be a set of n' = f(n, p, k) (reconfigurable spine-layer) switches, where each switch  $sw_i \in SW$  internally connects its in-out ports via a *matching* of size  $\leq p$ .

Let  $\mathcal{P}(sw_x) \subseteq V \times V$ ,  $|\mathcal{P}(sw_x)| = p^2$  be the (static) *in-out* port-set of a spine-layer switch  $sw_x \in SW$ .

Given a network topology  $N_t \in \mathcal{N}$  at time t, the objective is to find a set of switches SW, a set of matchings  $\mathcal{M}_t = \bigcup_{sw_x \in SW} M(x,t) = N_t$ , and all in-out port sets  $\mathcal{P}(sw_x), sw_x \in SW$ , such that  $\forall (u,v) \in N_t$ :

$$\exists sw_x \in SW \mid (u, v) \in M(x, t) \text{ and } M(x, t) \in \mathcal{P}(sw_x).$$

**Time model:** In sequential SAN algorithms [4], [20], [23], each message  $\sigma_i$  is processed strictly after the previous one  $\sigma_{i-1}$  has been delivered. In this work we consider a concurrent execution scenario. We assume that time is divided into synchronous rounds, and each round consists of a constant number of time-slots. In a round, multiple (independent) nodes can make adjustments concurrently. We consider that nodes and communication between them are reliable.

**Cost Model:** Consider a sequence  $\sigma$  of m messages, a SAN algorithm  $\mathcal{A}$ , any initial network  $N_0 \in \mathcal{N}$ , and a message  $\sigma_i(s_i, d_i) \in \sigma$ , generated at time  $b_i$  and delivered at time  $e_i$ . In terms of time, one objective is to minimize the makespan:

$$Makespan(\mathcal{A}, N_0, \sigma) = \max_{1 \le i \le m} e_i - b_1.$$

Let us define the *adjustment cost adj*<sub>i</sub> as the number of adjustments performed by  $\mathcal{A}$  to deliver  $\sigma_i$  and the *service cost srv*<sub>i</sub> to be the price of routing the message along the (shortest) path  $dist_{N_{e_i}}(s_i, d_i), N_{e_i} \in \mathcal{N}$ . We assume that routing a message incurs a cost of 1 unit per hop. MM allows to define the adjustment cost in different ways, depending on e.g. particular OCS hardware specification:

Edge distance: The case where the adjustment cost is proportional to the number of replaced edges between each consecutive matchings of the same switch sw<sub>x</sub> ∈ SW. If the cost of a single edge is α, then the adjustment cost for the entire network is defined as:

$$linkAdj(N_{t-1}, N_t) = \alpha \sum_{sw_x \in SW} |M(x, t) \setminus M(x, t-1)|.$$

• Switch Cost: In this case, if a matching (switch) is reconfigured (adjusted), it costs  $\alpha$  regardless of the number of edge changes in the matching. Let  $\mathbb{I}_{S=S'}$  be an indicator

function that denotes if set S is equal to set  $S^\prime$  . Then the adjustment cost for the network is:

$$swAdj(N_{t-1}, N_t) = \alpha \sum_{sw_x \in SW} \mathbb{I}_{M(x,t) = M(x,t-1)}$$

Let  $t_{\max} = \max_{1 \le i \le m} e_i$ . Finally, we define the total service cost, total edge adjustment cost, total switch adjustment cost, and total work cost, respectively, as follows:

$$Srv(\mathcal{A}, N_0, \sigma) = \sum_{i=1}^{m} (dist_{N_{e_i}}(s_i, d_i) + 1), \quad (1)$$

$$\operatorname{LinkAdj}(\mathcal{A}, N_0, \sigma) = \alpha \sum_{t=1}^{\iota_{\max}} linkAdj(N_{t-1}, N_t), \quad (2)$$

$$SwAdj(\mathcal{A}, N_0, \sigma) = \alpha \sum_{t=1}^{t_{max}} swAdj(N_{t-1}, N_t), \qquad (3)$$

$$\operatorname{Cost}(\mathcal{A}, N_0, \sigma) = \operatorname{Srv}(\mathcal{A}, N_0, \sigma) + \operatorname{Adj}(\mathcal{A}, N_0, \sigma)$$
(4)

#### III. OPTICNET

OpticNet is a framework for implementing SAN algorithms in the TMT network architecture. Firstly, we describe how OpticNet solves the MM'-PMP problem. Then, we describe how SAN adjustments are implemented in OpticNet.

Firstly, we partition the set of spine-layer switches SW into two subsets, by type: *unit switches*  $(SW^{\cup})$  and *cross switches*  $(SW^{\times})$ , as follows:

$$SW = SW^{\cup} \cup SW^{\times}.$$

For simplicity, we assume that n% p = 0 (or, equivalently, that  $1 \le x < p$  non-active vertices are added to the network, so that n is a multiple of p). Next, we partition the set of leaf-layer switches (ToRs) V into  $C = \left\lceil \frac{n}{p} \right\rceil$  clusters  $C_i \subseteq V, |C_i| = p$ , as follows:  $\forall (u, v) \in V \times V$ , if u < v then  $u \in C_i, v \in C_j$ , where:

$$i = \min\left(\left\lfloor \frac{u}{p} \right\rfloor, \left\lfloor \frac{v}{p} \right\rfloor\right), \ j = \max\left(\left\lfloor \frac{u}{p} \right\rfloor, \left\lfloor \frac{v}{p} \right\rfloor\right).$$

Each cluster  $C_i$  will be assigned to a group of k switches in  $SW^{\cup}$ , and each pair of clusters  $(C_i, C_j), i \neq j$  will be assigned to a group of 2k switches of type  $SW^{\times}$ . Finally, we define the in-out port-sets as follows:

$$\mathcal{P}(sw_{i \cdot k+x}^{\cup}) = C_i \times C_i, \ \forall \ 0 \le i < C, 0 \le x < k,$$

 $\mathcal{P}(sw_{idx(i,j)+x}^{\times}) = C_i \times C_j, \ \forall \ 0 \le i < j < C, 0 \le x < 2k,$ 

where:

$$idx(i,j) = 2k \cdot \sum_{x=0}^{i-1} (C-x-1) + 2k \cdot (j-i-1)$$
  
=  $k \cdot i \cdot (2 \cdot C - 1 - i) + 2k \cdot (j-i-1)$ 



Fig. 1. a) Full-duplex OpticNet TMT Architecture: Leaf Layer: constant-degree  $\leq k$  network on n nodes; Spine Layer: set of unit and cross-type p in-out port OCS switches  $SW = SW^{\cup} \cup SW^{\times}, |SW^{\cup}| = kC, |SW^{\times}| = 2k \cdot {C \choose 2}, C = \lceil n/p \rceil$ . (b) Full-duplex Unit switch example for a k = 4- degree network with n = p = 8.

The total number of spine-layer *p*-port switches to connect n leaf-layer switches in a constant-degree  $\leq k$  network used by OpticNet is<sup>3</sup>:

$$|SW| = |SW^{\cup}| + |SW^{\times}| = kC + 2k\binom{C}{2} = kC^2.$$
 (5)

In Figure 2a we illustrate how OpticNet implements a TMT architecture in a datacenter comprised of a k-degree network topology on n racks and a set of p-port spine-layer switches. A set of leaf-layer (ToR) switches is partitioned into C clusters of size p, and each  $v \in C_i$  is connected to one input and one output port of k unit switches, and to either one input or one output port of 2k cross switches, for each cluster  $C_j, j \neq i$ . The number of ports of each ToR switch is  $2k + 2k(C-1) = 2k \cdot C$ . Note that, for each cross cluster  $C_i \times C_j$ , half the switches would have vertices from  $C_i$  on the input ports and the vertices from  $C_j$  on the output ports, with the other half inverted. In Figure 1b we illustrate an example of four p = 8-port unit switches connecting a k = 4-degree network of n = 8 nodes. In Figure **??** we illustrate a BST network on n = 8 nodes, connected via 8 unit and 4 cross p = 4-port switches.

Network adjustments: We assume that, at each round t, OpticNet receives a set of edges  $new\_edges \leftarrow N_{t+1} \setminus N_t$  to be inserted, and a set of edges  $delete\_edges \leftarrow N_t \setminus N_{t+1}$ to be deleted, between two consecutive network topologies  $N_t \in \mathcal{N}$  and  $N_{t+1} \in \mathcal{N}$ . We denote by  $\mathcal{M}_t, \mathcal{M}_{t'}, \mathcal{M}_{t+1}$ the sets of matchings before, during and after the network adjustment operation, respectively. Initially, we set  $\mathcal{M}_{t'} \leftarrow \mathcal{M}_t$  and  $\mathcal{M}_{t+1} \leftarrow \mathcal{M}_t$ , and remove all edges in  $delete\_edges$ from  $\mathcal{M}_{t'}$  and  $\mathcal{M}_{t+1}$ . Then, each edge  $(u, v) \in new\_edges$ is added to some matching  $M(x, t+1) \in \mathcal{M}_{t+1}$ , as described below. Algorithm 1 describes the procedure of adding a single directed edge  $(u, v) \notin N_t$  to  $\mathcal{M}_{t'}$ . Firstly, from the subset of k unit or 2k cross switches  $S_u^v = \{sw_z \in SW | \mathcal{P}(sw_z) = C_i \times C_j, u \in C_i, v \in C_j\}$ , two switches, to which we refer as opposite switch pair, are selected: one, where an input port uis free  $(sw_x)$  and one in which the output port v is free  $(sw_y)$ (lines 1 - 6). Note that it is possible that  $sw_x = sw_y$ , but at least one  $sw_x$  and one  $sw_y$  must exist. Otherwise the addition of (u, v) would imply degree > k for u or v in  $N_{t+1}$ .

The algorithm works around the idea of an augmenting path between the pair of *opposite* matchings  $M(x, t') \in \mathcal{M}_{t'}$  and  $M(y,t') \in \mathcal{M}_{t'}$ , on switches  $sw_x$  and  $sw_y$ , respectively (lines 8-20). The Boolean variable *check\_out* is initially set to *true* (line 7), because we have to check for conflict (adjacent edge) on the output port v of switch  $sw_x$ . (It will be set to false when the input port of some switch needs to be checked for a conflict). Note that, by choice of  $sw_x$ , we know that u does not have a neighbor in  $sw_x$ , otherwise, its input port would not be available. So it is sufficient to check the v node's neighbors (lines 09-14). If there is a conflict, we remove the conflicting edge  $(w, v) \in M(x, t')$  and set *check\_out* to false. In the next iteration, we add (w, v) to the opposite matching M(y, t') and (since *check\_out* is false) check for conflict on the input port w of  $sw_y$  (lines 15-20). Note that there can be only one conflicting port at a time (either on the output or on the input of the switch). This process is repeated  $\leq 2(p-1)$  times until there are no more conflicting edges in the matchings M(x, t')or M(y, t') (line 08).

**Batch editing:** Algorithm 2 adds an optimization to Algorithm 1 when multiple edges are inserted at once (e.g., a bidirectional edge in the case of half-duplex switches, or a set of edges comprising one topological adjustment, such as a splay). New edges are inserted iteratively. Each edge  $(u, v) \in new\_edges$  is inserted into an intermediate network state  $\mathcal{M}_{t'}$  by making a call to Algorithm 1 (lines 3 - 5). Then all edges in  $\mathcal{M}_t \setminus \mathcal{M}_{t'}$  are removed from  $\mathcal{M}_{t+1}$  (lines

<sup>&</sup>lt;sup>3</sup>In the special case p < k, we can replace k by p in Eq. (5), because since there are at most p nodes per cluster, (k - p - 1) neighbors of each node in that cluster will belong to other clusters.

6-7), and all edges in  $\mathcal{M}_{t'} \setminus \mathcal{M}_t$  are added directly to  $\mathcal{M}_{t+1}$  (lines 8–9). In this way, when inserting several edges on the same switches, many updates become redundant. In particular, instead of  $\leq 2p$  updates per inserted edge *ie*, we have p times the number of updated switches, sw'. Note that,  $p * sw' \leq 2 * p * ie$  for any set of inserted edges.

Lazy adjustments: Even though batch-editing reduces the reconfiguration cost of simple operations, like splaying, an even greater gain can be achieved in Lazy SANs [23], in which topology reconfigurations are performed less often, or in socalled epochs. During one epoch, the physical network remains unmodified, while adjustments are performed on a copy of the network graph, and after each epoch, both network versions are synchronized.

## Algorithm 1 AugPath(): single edge insertion

**Require:**  $\mathcal{M}_{t'}, SW^{\cup}, SW^{\times}, k, (u, v) \notin N_t, u \in C_i, v \in C_j.$ 1: if i = j then %(unit switch)  $S_u^v \leftarrow \{sw_z \in SW^\cup | \ i \cdot k \le z < (i+1) \cdot k\}$ 2: else %(cross switch) 3:  $S_u^v \leftarrow \{ sw_z \in SW^{\times} | idx(i,j) \le z < idx(i,j) + 2k \}$ 4: 5:  $sw_x \leftarrow sw_z \in S^v_u | (u, w) \notin M(z, t') \in \mathcal{M}_{t'}, \forall w \in C_j$  $s_{i} sw_{u} \leftarrow sw_{z} \in S_{u}^{v}|(w,v) \notin M(z,t') \in \mathcal{M}_{t'}, \forall w \in C_{i}$ 7: check out  $\leftarrow$  true while  $(u, v) \notin (M(x, t') \cup M(y, t'))$  do 8: if *check\_out* then 9: add (u, v) to M(x, t')10: if  $\exists w \in C_i / \{u\}, (w, v) \in M(x, t')$  then 11:  $check\_out \leftarrow false$ 12: remove (w, v) from M(x, t')13:  $(u, v) \leftarrow (w, v)$ 14: else 15: add (u, v) to M(y, t')16: if  $\exists w \in C_j / \{v\}, (u, w) \in M(y, t')$  then 17:  $check\_out \leftarrow true$ 18: remove (u, w) from M(y, t')19:  $(u,v) \leftarrow (u,w)$ 20 21: return  $\mathcal{M}_{t'}$ 

### A. OpticNet framework implementation

We implemented OpticNet as a simulation framework for SAN algorithms in the context of TMT architectures, on top of which an interested party can easily add or extend the decision making and network adjustments specification of their SAN algorithm. Like some of the earlier work on concurrent SANs [26], [29], we adopt an optimistic approach to solve concurrency conflicts. Messages that have been in the network for longer are prioritized to avoid deadlocks and starvation.

Centralized control node: All communication between the leaf and the spine layers is implemented via a centralized controller node, that maintains a current global view of the network topology and coordinates port-mapping decisions among ToR and OCS switches. Moreover, the controller node

## Algorithm 2 BatchEdit(): set-of-edges insertion

**Require:**  $\mathcal{M}_t, SW^{\cup}, SW^{\times}, k, new\_edges.$ 1:  $\mathcal{M}_{t'} \leftarrow \mathcal{M}_t$ 2:  $\mathcal{M}_{t+1} \leftarrow \mathcal{M}_t$ 3: for  $(u,v) \in new\_edges$  do if  $(u, v) \notin M(z, t'), \forall M(z, t') \in \mathcal{M}_{t'}$  then 4:  $\mathcal{M}_{t'} \leftarrow \text{AugPath}(\mathcal{M}_{t'}, SW^{\cup}, SW^{\times}, k, (u, v))$ 6: for  $(u,v) \in M(z,t) \in \mathcal{M}_t \mid (u,v) \notin M(z,t') \in \mathcal{M}_{t'}$ do remove (u, v) from  $M(z, t+1) \in \mathcal{M}_{t+1}$ 7:  $(u,v) \in M(z,t') \in \mathcal{M}_{t'} \mid (u,v) \notin M(z,t) \in \mathcal{M}_t$ 8: **for** do

9: add 
$$(u, v)$$
 to  $M(z, t+1) \in \mathcal{M}_{t+1}$ 

10: return  $\mathcal{M}_{t+1}$ 

handles prioritization rules among nodes participating in current adjustment or service (routing and forwarding) operations, to ensure that they don't participate in conflicting operations.

Rounds and time-slots: The simulation is divided into synchronous rounds, and a message travels up to one hop per round. Each round is divided into 4 time-slots, as follows:

- nodeInformStep: Leaf-layer (ToR) switches (nodes) inform the controller node if they have messages to send;
- controllerStep: The controller node receives the network messages and computes the current round adjustment operations, informing all leaf and spine-layer switches which edges they must alter, and the network nodes about their new neighbors (e.g., children or parent), and grants permission to selected nodes to forward their messages;
- nodeRoutingStep: The nodes that received permis-• sion to forward their messages do so;
- logRoundResults: Network nodes receive their messages, inform the controller node if they are their message's final destination, and the controller node logs all relevant information about that round.

Multi-round adjustments: In the case of BST-based SANs, most adjustments take 2 rounds, and some (e.g. a zig-zag splay) take 3 rounds. In order to increase concurrency, OpticNet handles conflicts around such adjustments differently from some previous work [28]. Nodes participating in an adjustment operation are not locked for more than one round. To prevent multi-round adjustments from being interrupted by messages with higher priority, messages related to unfinished adjustments receive maximum priority.

**OpticNet-SAN integration:** The integration of OpticNet with SAN algorithms basically involves three steps. First one needs to create a new controller node class that inherits from the NetworkController class, add a constructor for it with the SAN algorithm specifications and a call to the parent class constructor. Then all decision making and attribute updating specific to the SAN algorithm (e.g., rank computation, path weight update or random number generation, in the case of a CBNet [29] implementation) is implemented as an override of the adjustment operations or message handling. Finally, it is needed to create a CustomGlobal class that will be responsible for calling the network constructor, firing messages into the network, defining the stop condition and any simulation configuration specifications.

**Source code:** We made the source code of the Optic-Net implementation available at https://github.com/ caiocaldeira3/OpticalNet. Note that, in this implementation, we assume  $\mathcal{N}$  to be the family of all BSTs, and switches to be half-duplex, so each switch has a reversed (mirrored) copy added to the spine layer. Examples of SANs algorithms implemented over OpticNet are provided further on.

## IV. BSTOPTICNET

SAN algorithms based on splaying adjustments [4], [28] assume that  $N_t$  is a BST. It is possible to utilize special properties of the BST graph to reduce the number of switches a cross cluster need. Similarly, it is also possible to remove the need of the augmenting path algorithm for edge insertions as well as of iterating over switches for edge indexing. These optimizations are free for cross clusters. However they incur an increase in the number of switches a unit cluster utilizes.

Firstly, it is important to note that, while the degree of our network is k = 3, the induced subgraph made by the union of matchings in the cross switches can have, at most, a degree of 2. This is in fact the case here because, given two clusters  $C_i$  and  $C_j$ , if i < j each vertex u from  $C_i$  will be smaller than any vertex v from  $C_j$ . This means that u can have only one child and parent from  $C_j$  at a given point. Since we can ensure the maximum degree of a cross cluster is at most 2, it is possible to represent it with only four switches instead of six, which would be the case for a regular graph of constant degree k = 3, resulting in  $|SW|_{BST} = 3C + 4\binom{C}{2} = C(2C + 1)$ .

#### A. Mirroring Switches

In practical scenarios the cost of reconfigurations can be much greater than that of routings. This provides incentive to minimize the number of reconfigurations your system performs at a given moment. For cross switches it is possible to structure our edges to make it so that edge indexing can be computed with a static math operations, and that edge insertions require only two link reconfigurations.

This abstraction requires us to split the 4 switches we use representing cross clusters into two pairs of Downward and Upward switches. The directed edges (u, v) where u is the parent of v will be contained in Downward Switches and the directed edges (u, v) where u is a child of v will be contained in Upward Switches. This way we can assign all left edges to a pair of Downward and Upward switches and all right edges to the other pair of Downward and Upward switches.

It is easy to see that this configuration is valid, since each vertex can have at most one left child its input and output ports on the Downward and Upward switches for left edges respectively will always be available when inserting an edge. Similarly, since each vertex can have at most one parent, its output and input on the Downward and Upward switches for left edges respectively will always be available when inserting an edge. This works analogously for right edges. Given that we group Downward and Upward switches similarly for all cross clusters, those with left edges followed by those with right edges for example, edge indexing can be performed with only one static math operation.

With Mirror Switches the benefits of applying Batch-Edit would be reserved to lazy reconfigurations, as there would not be conflicting paths between inserting edges. Also, while using the regular edge representation, given that splays have one edge reconfiguration that is simply a change of parenthood, no link would be required to be replaced. This is not the case for Mirror Switches. A change of parenthood means a change between a left or right edge; a change of switches is, therefore, required. However, this extra edge reconfiguration normally will not represent more link changes than the p factor involved in the augmenting path algorithm.

## B. Unit Cluster Mirroring

Furthermore, it is also possible to apply the same logic to unit clusters if we use four switches, instead of three, to represent them. This would result in  $|SW|_{BST} = 4C+4\binom{C}{2} = C(2C+2)$  clusters. The increase in cost is linear on the number of clusters whereas the number of switches involved in a splay is divided by half, and the number of link updates divided by p.

To summarize, it is important to take into account the specifics of your system when deciding which implementation of unit and cross clusters to use for a BST reconfigurable algorithm. Switch and link reconfiguration costs as well as budget to acquire new switches can influence which approach may be optimal for your system.

In Figure 1b we illustrate an example of four p = 8-port unit switches connecting a k = 4-degree network of n = 8nodes. In Figure **??** we illustrate a BST network on n = 8nodes, connected via 8 unit and 4 cross p = 4-port full-duplex switches.

#### V. ANALYSIS

In this section we analyze the correctness and optimality of OpticNet in the MM'. First we prove that Algorithm 1 terminates and correctly inserts new edges into the network.

**Lemma 1.** Let  $\mathcal{N}$  be the family of constant degree  $(\leq k)$ graphs on a set V of n nodes. Let  $SW = SW^{\cup} \cup SW^{\times}$  be the set of spine-layer p-port switches,  $\mathcal{M}_t = N_t \in \mathcal{N}$  be the set of matchings computed by OpticNet at time t, and let  $(u, v) \notin N_t$ be a directed edge to be inserted. If  $N_t \cup \{(u, v)\} \in \mathcal{N}$  then Algorithm 1 terminates in at most 2(p-1) iterations and returns a new set of matchings  $\mathcal{M}_{t'} = N_t \cup \{(u, v)\} \in \mathcal{N}$ , such that  $\exists sw_x \in SW \mid (u, v) \in M(x, t') \in \mathcal{M}_{t'}$ .

*Proof.* OpticNet assigns either  $2k \ cross$  (if  $i \neq j$ ) or  $k \ unit$  (if i = j) switches  $sw_z \in SW \mid \mathcal{P}(sw_z) = C_i \times C_j, u \in C_i \subseteq V, v \in C_j \subseteq V$ .



Fig. 2. Difference between Mirrored and Generic Optical Net representation for a BST with 8 vertices and k = 4

Since the out-degree of u and the in-degree of v must be  $\langle k \text{ in } N_t$ , there must exist at least one switch  $sw_x \in S_v^u$  (represented by  $M(x,t) \in \mathcal{M}_t$ ) such that the input port u is free, and at least one  $sw_y \in S_v^u$  (represented by  $M(y,t) \in \mathcal{M}_t$ ) such that the output port v is free. If x = y, then  $M(x,t') \leftarrow M(x,t) \cup \{(u,v)\}$ , and we are done.

If  $x \neq y$ , let  $M = M(x,t) \cup M(y,t) \cup \{(u,v)\}$ . Since  $|M| \leq 2(p-1) + 1$  and each port  $w \in C_i \cup C_j$  appears at most twice in M, M can be partitioned into two disjoint matchings M(x,t') and M(y,t') of size  $\leq p$ , as described in Algorithm 1 (lines 7-20).

The algorithm works around the idea of an augmenting path between matchings M(x,t) and M(y,t), on switches  $sw_x$  and  $sw_u$ , respectively. The Boolean variable *check\_out* is initially set to true (line 7), because we have to check for conflict (adjacent edge) on the output port v of switch  $sw_x$ . (It will be set to *false* when the input port of some switch needs to be checked for a conflict). Note that, by choice of  $sw_x$ , we know that the input port u is free on  $sw_x$ , so it is sufficient to check for conflict on the output port v of  $sw_x$ . If there is a conflict, we remove the conflicting edge  $(w, v) \in M(x, t)$ (leaving the input port w free on  $sw_x$ ) and set *check\_out* to false. In the next iteration, we add (w, v) to M(y, t) (where the output port v is free, by choice of  $sw_{u}$ ) and (since check\_out is false) check for conflict on the input port w of  $sw_y$ . If there is another conflict, edge  $(w, w') \in M(y, t)$  is moved to M(x,t). Note that there can be only one conflicting port at a time (either on an output or on an input port), and it will have been left free on the other switch in the previous iteration.

Since the augmenting path does not have repeated vertices (since M is comprised of two sets of  $\leq (p-1)$  independent edges), this process is repeated  $\leq 2(p-1)$  times until Mhas been partitioned into two disjoint matchings M(x,t') and M(y,t'). For contradiction, suppose there are 2(p-1)+1 =(2p-1) conflicting edges in the augmenting path. The (2p-1)1)st edge would have to be of the form  $(u,w) \in M(x,t)$ , which contradicts the choice of  $sw_x$  as having the u inputport free (and the fact that  $|M(x,t)| \leq (p-1)$ ). We now prove that OpticNet can represent any network  $N_t \in \mathcal{N}$  at time t, i.e., every edge is assigned to a matching on some switch.

**Theorem 1.** Let  $\mathcal{N}$  be the family of constant degree  $(\leq k)$ graphs on a set V of n nodes. Let SW be a set of spine-layer p-port switches and  $\mathcal{M}_t = N_t \in \mathcal{N}$  be the set of matchings computed by OpticNet at time t. We have that  $\forall (u, v) \in V \times V$ , if  $(u, v) \in N_t$ , then  $\exists sw_x \in SW \mid (u, v) \in M(x, t) \in \mathcal{M}_t$ .

*Proof.* W.l.g, we assume that edges are directed, i.e., switches are half-duplex. The proof is by induction on the number of edges.

*Base case:* If  $N_t$  has no edges, the claim is vacuously true since  $(u, v) \notin N_t, \forall (u, v) \in V \times V$ .

 $\begin{array}{l} \textit{I.H.: } \forall (u',v') \in V \times V, \text{ if } (u',v') \in N'_t = N_t \setminus (u,v) \text{ then } \\ \exists sw_{x'} \in SW \mid (u',v') \in M(x',t), \ M(x',t) \in \mathcal{M}'_t = N'_t. \end{array}$ 

By I.H., every edge in  $N'_t$  is assigned to some matching in  $\mathcal{M}'_t$ . Consider an edge  $(u, v) \notin N'_t$  such that  $N_t = N'_t \cup \{(u, v)\} \in \mathcal{N}$ , i.e., the insertion of the new edge preserves degree  $\leq k$  of the underlying graph. By Lemma 1, Algorithm 1 returns a set of matchings  $\mathcal{M}_t = N_t$ , such that  $\exists sw_x \in SW \mid (u, v) \in \mathcal{M}(x, t) \in \mathcal{M}_t$ . This concludes the proof.

The following theorem proves the correctness for the special case of BST.

**Theorem 2.** Let  $T_t$  be any BST on n nodes at time t, and let SW and  $\mathcal{M}_t$  be the set of spine-layer p-port switches and the set of matchings computed by OpticNet. If  $(u, v) \in T_t$  then  $\exists sw_x \in SW | (u, v) \in M(x, t), M(x, t) \in \mathcal{M}_t$ .

*Proof.* Case 1 (cross switch,  $i \neq j$ ): Since the induced subgraph made from the vertices within  $C_i$  and  $C_j$  and only the edges that connect them on a BST have a constant degree of 2. This proof follows from the case 1 on Theorem 1

**Case 2 (unit switch,** i = j): W.l.g, this proof follows from Theorem 1.

We proceed by showing that the number of spine-layer switches is optimal.

**Theorem 3.** Let  $\mathcal{N}$  be the family of constant degree  $(\leq k)$  graphs on a set V of n nodes, and OPT we the minimumsize set of spine-layer switches with p in-out ports needed to connect n leaf-layer switches via a TMT two-layer architecture in the MM'. Let SW be a set of spine switches computed by OpticNet and  $C = \left\lceil \frac{n}{p} \right\rceil$ , then

$$|OPT| \ge |SW| = C^2 \left\lceil \frac{k}{2} \right\rceil$$

*Proof.* For simplicity sake, we assume that loop edges are possible  $(v, v), \forall v \in V$  in some network topologies  $N_t \in \mathcal{N}$ . Let OPT be any feasible solution for the MM'-PMP. Let

 $\mathcal{P}(sw_i) \subseteq V \times V, |\mathcal{P}(sw_i)| \leq p^2$  be the (static) *in-out port*set of a spine-layer switch  $sw_i \in OPT$ . Let  $\mathcal{P}(v)$  be the port-set of a leaf-layer switch  $v \in V$ . And let  $\mathcal{P}(OPT) = \bigcup_{sw_i \in OPT} \mathcal{P}(sw_i)$  and  $\mathcal{P}(V) = \bigcup_{v \in V} \mathcal{P}(v)$  be the (total) portsets of spine and leaf layers, respectively.

Note that there must be a one-to-one assignment between leaf and spine-layer ports, so  $|\mathcal{P}(OPT)| \ge |\mathcal{P}(V)|$ . Moreover, since each spine switch connects  $p^2$  in-out port pairs, we have:

$$|OPT| \ge \frac{|\mathcal{P}(OPT)|}{p^2} \ge \frac{|\mathcal{P}(V)|}{p^2}$$

At any time t, each leaf switch  $v \in V$  might need k simultaneous connections to any subset of k nodes out of n. So we have that  $\mathcal{P}(v) \geq k \cdot n, \forall v \in V$ . Since edges are not directed (full-duplex), it follows that:

$$|OPT| \ge \frac{\mathcal{P}(V)}{p^2} \ge \left\lceil \frac{k}{2} \right\rceil \cdot \frac{n^2}{p^2} \ge C^2 \left\lceil \frac{k}{2} \right\rceil.$$

Finally, we show that any SAN algorithm runs on top of OpticNet, preserving the total cost guarantees.

**Theorem 4.** Let  $\mathcal{N}$  be the family of constant degree  $(\leq k)$ graphs on a set of n nodes. Consider any initial  $N_0 \in \mathcal{N}$ , a sequence of m messages  $\sigma$  and a SAN algorithm  $\mathcal{A}$ . Let SW be the set of spine-layer p-port switches and  $\mathcal{M}_t = \bigcup_{sw_x \in SW} \mathcal{M}(x, t)$  be the set of matchings computed by OpticNet at time t, such that  $\mathcal{M}_t = N_t \in \mathcal{N}$ . The total service, edge and switch adjustment, and work costs incurred by  $\mathcal{A}$  on top of OpticNet to deliver all messages in  $\sigma$  are:

$$Srv(OpticNet(\mathcal{A}), N_0, \sigma) = Srv(\mathcal{A}, N_0, \sigma),$$
  

$$LinkAdj(OpticNet(\mathcal{A}), N_0, \sigma) \leq 2p \cdot LinkAdj(\mathcal{A}, N_0, \sigma),$$
  

$$SwAdj(OpticNet(\mathcal{A}), N_0, \sigma) \leq 2 \cdot LinkAdj(\mathcal{A}, N_0, \sigma),$$
  

$$Cost(OpticNet(\mathcal{A}), N_0, \sigma) = O(Cost(\mathcal{A}, N_0, \sigma)).$$

*Proof.* An adjustment operation can be defined in terms of a set of edges to be removed or added to a network topology at each time t. Algorithm 1 implements an edge-addition operation with cost  $\leq 2p$  using the *edge-distance* metric and cost  $\leq 2$  using the *switch-cost* metric. Therefore, the

asymptotic amortized cost of a SAN algorithm based on splaying, such as SplayNet [4], DiSplayNet [26] or CBNet [28], combined with OpticNet, remains the same.  $\Box$ 

## A. Mirror Switches

**Theorem 5.** Let  $T_t$  be any BST on n nodes at time t, let  $\mathcal{M}_t$  be the set of matchings computed by OpticNet. Be  $SW_m$  the set of mirrored switches of a given cluster  $C_i$  and  $(u, v) \in T_t$  such that  $u, v \in C_i$ . Then  $\exists sw_x \in SW^M | (u, v) \in$  $M(x, t), M(x, t) \in \mathcal{M}_t$ 

*Proof.* Case 1 (Downward, u is parent of v) Let  $SW^D \in SW^M$  the set of Downward switches and  $SW^D = \{SW_L^D, SW_R^D\}$ . W.l.g, let's assume that u > v. Suppose v's output port is occupied, this would imply that  $\exists (w, v) \in SW_L^D | w \neq u$ , this is a contradiction since v can have at most one parent. Suppose on the other hand that u's input port is occupied, this would imply that  $\exists (u, w) \in SW_L^D | w \neq v$ , this is a contradiction since u can have at most one left child.

**Case 2** (Upward, u is child of v) Let  $SW^U \in SW^M$ the set of Upward switches and  $SW^U = \{SW_L^U, SW_R^U\}$ . W.l.g, let's assume that u < v. Suppose u's input port is occupied, this would imply that  $\exists (u, w) \in SW_L^U | w \neq v$ , this is a contradiction since u can have at most one parent. Suppose on the other hand that v's output port is occupied, this would imply that  $\exists (w, v) \in SW_L^U | w \neq u$ , this is a contradiction since v can have at most one left child.

#### VI. EVALUATION

In this section we present our experimental results. We implemented three SAN algorithms on top of OpticNet:

- SN<sup>4</sup>: SplayNet [4], [30] centralized and sequential generalization of a splay tree;
- DSN: DisplayNet [26] distributed and concurrent version of SplayNet;
- CBN<sup>5</sup>: CBNet [29] distributed and concurrent generalization of CBTrees [27].

We used the following metrics, defined in Section II, to evaluate the simulation results:

- *Service cost*: the number of times a message was shared between adjacent nodes in the path from it's source to it's destination, we also compute the number of times a node, switch or input port was part of a routing operation.
- Adjustment edge-distance cost: the number of ports that were altered in an adjustment, caused by a message. For example, zig-zig rotation requires up to 8\*p link changes and a zig-zag requires up to 16 \* p link updates.
- Adjustment switch cost: the number of switches whose ports were altered. For example, a *zig-zig* rotation requires up to 8, and a *zig-zag* requires up to 16 switch updates.
- *Throughput*: the average number of delivered messages per round.

<sup>&</sup>lt;sup>4</sup>https://github.com/caiocaldeira3/SemiDisplayOpticNet <sup>5</sup>https://github.com/caiocaldeira3/CBOpticalNet

- Activity: the number of times a node, port, switch or request has been used in a routing or adjustment operation.
- *Total work*: the total number of routing and adjustment operations in the network.

#### A. Workload traces

To measure the locality of reference present in a workload, we use the definition of *trace complexity* [16], which leverages only randomization and data compression operations. The amount of locality present in a workload can be measured based on the entropy of the communication sequence. The concept of entropy is related to the amount of information or the ability to compress the data. Intuitively, workloads with a low locality structure tend to have random sequences of communication pairs and, consequently, a low data compression rate. High-locality sequences tend to have a specific structure between requests that allows for better compression. In particular, we distinguish temporal and non-temporal components.

We used the following workload traces in our experiments, grouped according to their locality characteristics:

- High non-temporal and low temporal: ProjectToR [31] describes the communication probability distribution among 8,367 pairs of nodes in a network of n = 128 nodes (top of racks), randomly selected from 2 production groups, executed between map-reduce operations, index builders, database and storage systems. We sample a sequence of m = 10,000 independent orders and identically distributed (*i.i.d.*) in time by the given communication matrix and repeat each experiment 30 times. Skewed corresponds to an artificial sequence of 10,000 communication requests in a network of n = 128 nodes, using the method from [16]. The non-temporal locality component was produced using the Zipf distribution.
- High temporal and low non-temporal: The traces of **PFabric** [32] were generated by executing simulation scripts in NS2. We sample a sequence of m = 1,000,000 requests from a network of 144 nodes. **Bursty** was generated artificially with m = 10,000 and n = 128, using the method from [16].
- Low locality: The Facebook trace consists of real *Fbflow* packets collected from the production clusters of Facebook. The per-packet sampling is uniformly distributed with rate 1:30000, flow samples are aggregated every minute, and node IPs are anonymized. We mapped the anonymized IPs to a consecutive value range starting at 0. This resulted in a sequence of 1,000,000 requests, originated in a 24-hour time window, in a network comprising 159 nodes.

To space the requests in time and make the timestamp sequences more realistic, we used a Poisson distribution with  $\lambda = 0.25$  to determine the time of the entrance of each message in the network.

## B. Results

**Total work and throughput:** In Figures 3 and 4, we can see blackthe total work and throughput for all workloads.

Note that these metrics are not affected by the OpticNet framework. What we can observe is that CBNet performs almost no adjustments, compared to SplayNet and DiSplaynet, and has a higher total (service) cost only in the Bursty workload. This is due to the extremely high temporal locality of this workload, which gives advantage to more aggressive reconfiguration algorithms, like SplayNet and DiSplayNet. We can also observe that the concurrent SANs have a much higher throughput than the sequential one (SN).

Activity: In Figures 5 and 6 we plot the CDFs of the percentage of active rounds and active ports per switch, for all workloads respectively, (except ProjecToR, which we discuss separately). In all plots, the smallest switch size was used (p = 8) for a network with  $n \in \{128, 144, 367\}$  nodes, so the number of switches was quite high  $(n' \in \{544, 684, 4324\})$ .

Analyzing the results in Figure 5, we observe that most of the switches experience a significant amount of idle time. This is more explicit when dealing with SAN algorithms with low levels of adjustment, such as CBNet. In most simulations, the up time of most switches does not go over 60% of rounds. In some cases most switches aren't even up in any round. With SAN algorithms that are more adjustment intensive, like SplayNet and DiSplayNet, we see that the switch activity is better distributed, and fewer switches have no up time.

Analyzing the results in Figure 6, which shows how many ports of a switch have been active at least in one round, we get similar results in nature, with CBNet presenting a higher concentration of active ports, while SplayNet and DisplayNet present a more balanced port activity among switches.

When comparing the network activity over the Bursty, Skewed, PFabric and Facebook datasets, we would like to point out that since splay operations typically involve more than one switches, we can see that DiSplayNet shows a more even distribution of active rounds per switch than CBNet. SplayNet, however, due to its sequential nature, presents lower percentiles than its distributed counter-part.

Another interesting observation is the discrepancy between active ports percentage between CBNet and DiSplayNet and SplayNet, with CBNet presenting a much higher concentration of active ports, even in the longer workload sequences (PFabric and Facebook, where m = 1,000,000). Over this longer sequences (Figures 6c and 6d), we also observe a congruence in the results for DiSplayNet and SplayNet.

**Variable switch size** (*p*): In Figures 7 and 8 we plot the CDFs of the percentage of active rounds and active ports per switch, for the ProjecToR workload, with a variable number of switch ports. We can analyze more carefully the impact of a greater number of switches on the network activity. We can see clearly, for example, that by increasing the switch size, the number of completely inactive switches drops dramatically. In particular, the cap for active port percentage of a switch for CBNet decreases with higher number of ports, while SplayNet and DisplayNet actually manage to distribute the workload more evenly over the different switch ports.



Fig. 3. Total work (all workloads): m = 10,000: (a) ProjecToR, (b) Bursty, (c) Skewed; m = 1,000,000: (d) Facebook, (e) PFabric.



Fig. 4. Throughput (all workloads): m = 10,000: (a) ProjecToR, (b) Bursty, (c) Skewed; m = 1,000,000: (d) Facebook, (e) PFabric.



Fig. 5. CDF Active rounds percentage per switch: constant switch size p = 8,  $n \in \{128, 144, 367\}$  (a) Bursty, (b) Skewed, (c) Facebook, (d) PFabric.



Fig. 6. CDF Active ports percentage per switch: constant switch size p = 8,  $n \in \{128, 144, 367\}$  (a) Bursty, (b) Skewed, (c) Facebook, (d) PFabric.

#### VII. RELATED WORK

Reconfigurable network topologies can be grouped in two basic types: demand-oblivious, e.g. [8], [9], [33], [34] and demand-aware, e.g. [3]–[5], [19], [24], [26], [35]–[40], or a combination of both, e.g., Cerberus [41]. Most existing demand-aware architectures rely on an estimation of traffic matrices [5], [17], [37], [38], [42], [43] which can limit the granularity and reactivity of the network, but there are also more fine-grained approaches such as [24], [35], which however rely on a centralized control.

The majority of datacenter networks with on-demand reconfigurations use full crossbar, 3D-MEMS-based OCS [18], or Wavelength Division Multiplexing-based switching [17]. Several prototypes based on OCS have been built, and their advantages demonstrated, e.g., the Helios prototype [5] uses a commercially available Glimmerglass OCS with 64 ports, while OSA [19] provides a testbed that consists of a Polatis Series 1000 32-port OCS. To operate such RDCNs efficiently, the self-adjusting network topology has to be mapped to a set of OCS dynamically in real-time.

While promising performance results have been demonstrated with various prototypes of demand-aware reconfigurable networks, today, it is often challenging to experiment with these technologies, as they are usually based on custombuilt prototypes and rely on tailored hardware and software which is not publicly available. One example of a framework that supports experimentation and reproducibility is ExReC [44]. It uses off-the-shelf hardware (Polatis Series 6000n  $32 \times 32$  OCS [25]) for evaluating different hybrid reconfigurable topologies and applications.

The closest work to ours is probably [23], where online strategies are proposed to adapt SAN algorithms for the matching model [22], based on spaced out (less frequent) network adjustments using existing (sequential) SAN algorithms, such



Fig. 7. ProjecToR: CDF Active rounds percentage per switch: variable switch size  $p \in \{8, 32, 64, 128\}, n = 128$ 



Fig. 8. ProjecToR: CDF Active ports percentage per switch: variable switch size  $p \in \{8, 32, 64, 128\}, n = 128$ .

as SplayNets [4] and ReNets [24].

## VIII. CONCLUSION

Even though emerging hardware reconfiguration technologies introduce an additional degree of freedom to the datacenter network design problem, they still face challenging system and algorithm design problems. Due to additional control logic and several milliseconds latency of the state-ofthe-art demand-aware optical switches, their cost can only be amortized for large flows over longer terms.

In this work, we used a synchronous distributed system model. OpticNet assumes a consistent and communicationclosed round structure provided by the distributed system. While many solutions to problems in distributed computing assume lock-step rounds, real-world distributed systems are usually not perfectly synchronous. In practice, message loss is present as a result of job dropping by a real-time scheduler or an unreliable communication channel.

While our contribution is still theoretical in nature, we believe it constitutes an interesting step forward toward practical self-adjusting networks. Our work opens interesting avenues for future research, such as considering implications on network and transport layers and understanding the trade-off between maximizing throughput and minimizing latency in both demand-aware and oblivious self-adjusting networks [34].

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